

# Multigraph-based Deep Programming Ability Tracing Method For Students

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Programming has become a crucial ability with the development of artificial intelligence, making it increasingly important to track and improve programming proficiency of students. However, most programming ability tracing methods rely primarily on the final outcomes of programming exercises to measure the programming proficiency, and neglect the rich behavioral structure information derived from the programming process, leading to a suboptimal solution in the programming ability tracing. To this end, we propose a multigraph-based deep programming ability tracing method for students (MDPAT), which consists of four components. Specifically, MDPAT devises the multigraph programming modelling via conducting the program knowledge graph and the program iteration graph to generate the submission representations of programming exercises, which effectively captures static structure information and dynamic structure information within the programming process. Then, MDPAT designs the programming knowledge gated update and the programming ability gated update to aggregate information of the programming knowledge and the programming ability that are derived from submission representations, which achieves a balanced and comprehensive tracking of evolving programming proficiency. Meanwhile, MDPAT utilizes the programming answer prediction to generate final programming proficiency measurement of students. Four components of MDPAT collaborate organically to achieve maximum performance in the programming ability tracing. Finally, extensive results on two real world datasets, especially on the Atcoder\_C dataset, ACC shows a 5.06% improvement compared to the second best result, verify that MDPAT conducts a new standard baseline in the programming ability tracing.

**Keywords:** Programming ability tracing; multigraph programming modelling; gated update learning

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## 1. Introduction

Knowledge tracing (KT) is an important research area focused on analyzing student knowledge states, and has recently gained attention from educators and researchers [1, 2]. KT captures changes in students' knowledge states through their historical answering records, allowing for the prediction of future problem-solving performance. It has been widely applied in various educational contexts, such as predicting career choices for students, forecasting potential errors in second language learning, and providing

course recommendations for university students. Traditional knowledge tracing models include item response Theory, bayesian knowledge tracing, and knowledge tracing based on factor analysis [3, 4]. While these models possess good interpretability, they rely on theoretical assumptions and require manual construction of input features. This often leads to limitations and biases, resulting in generally subpar predictive performance. In contrast, deep learning-based knowledge tracing models, such as Deep Knowledge Tracing, have shown significant improvements in predictive accuracy, utilizing advanced techniques such

as Recurrent Neural Networks [5], Memory Networks [6], Self-Attention Mechanisms [7], and Deep Neural Networks [8].

Although knowledge tracing has been widely applied in traditional course learning, programming learning possesses unique characteristics, primarily reflected in the following three aspects: Most programming problems do not have a single correct answer and often assess multiple knowledge points simultaneously, allowing students to provide open-ended solutions based on their learned knowledge [9–11]. The source code submitted by students contains semantic and syntactic information of the programming language, reflecting their mastery of the programming language and the relevant data structures and algorithms. For programming exercises, students typically need to modify and resubmit their code multiple times before successfully completing the problem [12–14].

With the increasing popularity of programming education, research efforts aimed at programming knowledge tracing have gradually increased. Wang et al. were the first to combine deep knowledge tracing models with student programming, using a recurrent neural network to analyze students' multiple attempts on the same exercise [9]. Although this model can capture students' knowledge states, it only considers code features and fails to utilize related features such as problems and knowledge points, overlooking the relationship between code and problems. Swamy et al. improved the code representation method based on Wang et al.'s work, but this approach requires building separate models for each knowledge point to analyze students' mastery of specific topics [10]. Jiang et al. proposed modeling students' multiple attempts on the same exercise by analyzing the abstract syntax tree edit distance sequences between students' submitted answers and the standard answers. However, this approach assumes that each problem has a corresponding standard answer [11].

Despite the progress made in programming skill tracing techniques, three major challenges remain: (1) Accurate representation of student-generated code: Existing code representation techniques are primarily designed for industrial-level code, lacking the adaptability required to capture the unique patterns in student submissions. More precise representations are essential to accurately model student programming behaviors and foundational understanding. (2) Comprehensive modeling of the iterative coding process: Students often engage in iterative problem-solving, refining their solutions based on feedback. Effective modeling of this iterative process, from initial solution formulation to subsequent adjustments, is crucial to understanding the evolution of programming proficiency. (3)

Granular assessment of programming ability: Programming assessments must go beyond knowledge recall and examine how students apply this knowledge to solve problems. A clear distinction between conceptual understanding and practical application is necessary to provide a more comprehensive and detailed evaluation of programming skills.

To this end, we propose a multigraph-based deep programming ability tracing method for vocational college students (MDPAT), which integrates multigraph programming modeling, gated updates for programming knowledge and ability, and programming answer prediction. MDPAT utilizes multigraph programming modeling to capture both static and dynamic structural information in the programming process, effectively identifying key relationships and patterns in the code, such as structural dependencies between code elements and the evolving changes in students' programming behavior across submissions. By incorporating gated update mechanisms for both programming knowledge and ability, MDPAT selectively aggregates relevant information from submissions, ensuring efficient integration of new knowledge while preserving important prior learning. This allows MDPAT to track programming proficiency comprehensively. Finally, in the programming answer prediction stage, MDPAT unifies programming knowledge and ability into a single predictive architecture, which considers both a student's knowledge mastery and their problem-solving ability, leading to improved prediction accuracy.

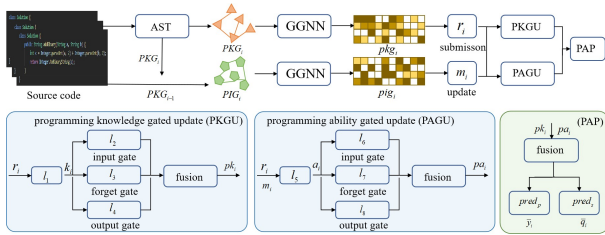
MDPAT makes several notable contributions, including:

- MDPAT models dual representation of both static and dynamic code features via multigraph learning, to capture the structural and temporal evolution of code, which enables a richer understanding of student learning patterns and leads to more precise assessments.
- MDPAT designs gated update mechanism to adaptively filter and update the knowledge state, selectively incorporating new submissions while maintaining continuity with prior knowledge. This dynamic retention of salient historical context supports more robust tracking of skill progression.
- Extensive results on two real world datasets, verify that MDPAT conducts a new standard baseline in the programming ability tracing.

## 2. Multigraph-based deep programming ability tracing method for students

Let the sequence of submissions about programming exercise by a student be denoted as  $R = \{r_1, r_2, \dots, r_n\}$ , where

each submission  $r_i = (e, c_i, y_i)$  represents a student's attempt  $c_i$  on exercise  $e$  at the  $i$ -th time. If the submission meets the exercise criteria,  $y_i$  is set to 1; otherwise, it is set to 0. The goal of the programming ability tracing is to evaluate the programming proficiency of students according to historical programming exercise records. To this end, we propose a multigraph-based deep programming ability tracing method for students in high vocational colleges, which consists of the multigraph programming modelling, programming knowledge gated update, programming ability gated update and programming answer prediction, as shown in Fig. 1.



**Fig. 1.** The illustration of MDPAT. MDPAT consists of the multigraph programming modelling, programming knowledge gated update, programming ability gated update and programming answer prediction

## 2.1. Multigraph programming modelling

Inspired by prior works [13, 14], we introduce the program knowledge graph and the program iteration graph to capture and represent code features and changes during programming practice. Specifically, PKG is designed to represent the static features of the code submitted by students. It begins with the construction of an Abstract Syntax Tree from the source code  $c_i$ , which provides a hierarchical structure that adheres to the syntax of the programming language. Each node in the PKG corresponds to a node in the AST, and edges represent the relationships between these nodes. The graph goes beyond the structure edges of the AST by introducing additional edges that represent data flow and error information, thus highlighting the unique characteristics of the student code. PIG is designed to capture the dynamic evolution of the code as students iterate their codes. It considers the sequence of codes submitted by students over time. The model analyzes the differences between consecutive submissions to identify changes such as additions, deletions, or modifications in the code. These changes are then represented as edges in the PIG, connecting nodes that represent successive submissions. The edges in the PIG are defined based on the presence of changes

between consecutive code submissions:

$$E_{PIG} = \{(v_i, v_j) \mid \Delta_{i,j} \neq \emptyset\} \quad (1)$$

where  $\Delta_{i,j}$  represents the differences identified by the function  $\text{diff}(r_t, r_{t+1})$ , which compares two submissions  $r_t$  and  $r_{t+1}$ .  $v_i$  and  $v_j$  denote nodes in PKG.

Graph-based representations are essential for understanding the structure and semantics of codes. Since the Gated Graph Neural Network (GGNN) can capture complex dependencies and relationships within graph-structured data and is suitable for code analysis tasks, we utilize GGNN to encode both local and global contextual information about the entire graph, for effectively extracting features from the program knowledge graph and the program iteration graph. Let  $PKG_i$  represent the program knowledge graph for code  $c_i$ , and  $PIG_i$  represent the program iteration graph. We use GGNN to extract representations from  $PKG_i$  and  $PIG_i$ , denoted as  $pkg_i$  and  $pig_i$ , respectively:

$$\begin{aligned} pkg_i &= \text{GGNN}(PKG_i) \\ pig_i &= \text{GGNN}(PIG_i) \end{aligned} \quad (2)$$

Then, the triplet  $(e, pkg_i, y_i)$  is viewed as the submission  $r_i$  at the  $i$ -th time. To represent the updated information for a submission, we consider the previous submission complete representation  $r_{i-1}$ , along with the modification representations  $pi_g_i$  for the current submission  $r_i$ . The updated information is denoted as  $m_i$ :

$$m_i = \text{fusion}(r_{i-1}, pi_g_i) \quad (3)$$

where  $\text{fusion}()$  denotes information aggregation function. The multigraph programming model introduces two key graph representations to capture and analyze code features and iterations. PKG represents the static structure of student code by building upon the Abstract Syntax Tree and adding edges for data flow and error information, while PIG captures the dynamic evolution of code through sequential submissions, with edges representing changes between versions. GGNN are used to encode both PKG and PIG, extracting meaningful representations of static and dynamic features. These representations are then combined to model the evolution of code, allowing the updated submission information to reflect both past and present changes, thus enabling comprehensive analysis of student code development over time.

## 2.2. Programming knowledge gated update

During the programming process, students construct their submissions to exercises by drawing upon their accumulated programming knowledge. Consequently, we leverage

the submission information to effectively refine and update programming knowledge.

Specifically, the update of the programming knowledge  $pk_i$  follows an LSTM-inspired structure, where the programming knowledge is progressively updated based on the current submission  $r_i$  and the previous programming knowledge  $pk_{i-1}$ . To achieve this, we first derive the new knowledge  $k_i$  from the current submission  $r_i$  using a nonlinear layer  $l_1$ , i.e.,  $k_i = l_1(r_i)$ . Next, we calculate the input gate  $I_i^{pk}$ , which determines how much of the new knowledge  $k_i$  should be incorporated. This is done by concatenating  $k_i$ , the previous programming knowledge  $pk_{i-1}$ , and position representations  $p_i$ , and then applying a nonlinear layer  $l_2$ :

$$I_i^{pk} = l_2([k_i, pk_{i-1}, p_i]) \quad (4)$$

Similarly, the forget gate  $F_i^{pk}$  is computed to control how much of the previous programming knowledge  $pk_{i-1}$  should be retained:

$$F_i^{pk} = l_3([k_i, pk_{i-1}]) \quad (5)$$

where  $l_3$  is another nonlinear layer. Lastly, the output gate  $O_i^{pk}$  is calculated to determine how much information is passed to the next state:

$$O_i^{pk} = l_4([k_i, pk_{i-1}]) \quad (6)$$

Then, the cell state  $\widetilde{pk}_i$  is updated by combining the forget gate with the previous knowledge and the input gate with the new knowledge:

$$\widetilde{pk}_i = F_i^{pk} \cdot pk_{i-1} + I_i^{pk} \cdot k_i \quad (7)$$

Finally, the programming knowledge  $pk_i$  is updated using the output gate, which integrates the current cell state and regulates the final output:

$$pk_i = O_i^{pk} \cdot \tanh(\widetilde{pk}_i) \quad (8)$$

This structure allows the model to selectively integrate new information from the current code submission while retaining relevant prior programming knowledge, similar to the gating mechanism of LSTM cells.

### 2.3. Programming ability gated update

In practice, initial submission often fails to meet the exercise requirements. After submitting programming code, students receive feedback to help them decide whether or not to modify their submissions. Therefore, we focus on the iterative refinement of source code submissions, referred to as the programming ability.

The update of the programming ability  $pa_i$  is structured similarly to an LSTM mechanism, where the programming

ability is iteratively updated based on the current submission  $r_i$  and the previous programming ability  $pa_{i-1}$ . The calculation of the new knowledge  $a_i$  is first performed by concatenating the current submission  $r_i$  and updated information  $m_i$ , followed by applying a nonlinear layer  $l_5$ , i.e.,  $a_i = l_5(r_i \oplus m_i)$ . Next, the input gate  $I_i^{pa}$  determines the extent to which information from the new submission should be integrated into the programming ability:

$$I_i^{pa} = l_6([a_i, pa_{i-1}]) \quad (9)$$

The forget gate  $F_i^{pa}$  regulates the retention of previous programming ability:

$$F_i^{pa} = l_7([a_i, pa_{i-1}]) \quad (10)$$

and the output gate  $O_i^{pa}$  dictates how much of the updated programming ability is carried forward to the next iteration:

$$O_i^{pa} = l_8([a_i, pa_{i-1}]) \quad (11)$$

The input gate controls the integration of new information, the forget gate manages the retention of previous abilities, and the output gate facilitates the passage of updated programming ability to the subsequent iteration. Next, the cell state  $\widetilde{pa}_i$  is updated by combining the contributions from the forget gate and the previous programming ability with the input gate:

$$\widetilde{pa}_i = I_i^{pa} \cdot pa_{i-1} + F_i^{pa} \cdot a_i \quad (12)$$

Finally, the programming ability  $ca_i$  is computed using the output gate, which integrates the current cell state and determines the final output:

$$pa_i = O_i^{pa} \cdot \tanh(\widetilde{pa}_i) \quad (13)$$

This architecture enables the model to effectively incorporate new information from the current solution while preserving relevant aspects of the prior programming ability, mirroring the gating mechanisms found in LSTM cells.

### 2.4. Programming answer prediction

After fitting programming knowledge and ability of students, a programming answer prediction network is designed via fusing programming knowledge and programming ability into a unified programming exercise architecture.

Initially, we derive the initial submission for the next exercise using the exercise requirement  $e_{i+1}$  and the current programming knowledge  $pk_i$ , i.e.,  $s_{i+1} = l_9([pk_i, e_{i+1}])$ . Next, we model programming exercise to form the answer  $a_{i+1}$ , which represents the source code, by utilizing the derived submission  $s_{i+1}$  and the programming ability  $pa_i$ ,

**Table 1.** MDPAT Algorithm Flow

|  |
|--|
| <b>Input:</b> Student sequence of submissions $R = \{r_1, r_2, \dots, r_n\}$                       |
| <b>Output:</b> Programming proficiency measurement $\bar{y}_i$ and $\bar{q}_i$                     |
| 1. For each submission $r_i = (e, c_i, y_i)$ :   |
| 2.     Construct program knowledge graph and program iteration graph.                              |
| 3.     Extract features using GGNN: $pkg_i \leftarrow GGNN(PKG_i), pig_i \leftarrow GGNN(PIG_i)$ . |
| 4.     Update submission information: $r_i = (e, pkg_i, y_i)$ .                                    |
| 5.     Update modification information: $m_i \leftarrow (r_{i-1}, pig_i)$ .                        |
| 5.     Extract programming knowledge $pk_i$ using gated mechanism.                                 |
| 6.     Extract programming ability $pa_i$ using gated mechanism.                                   |
| 7.     Predict the answer $a_i$ using current knowledge and ability.                               |
| 8.     Calculate final prediction $\bar{y}_i$ and $\bar{q}_i$ .                                    |
| 9.     Calculate the loss $L$ and optimize with SGD.   |
| 10. End.   |
| 11 Return: The model parameters and $\bar{y}_i$ and $\bar{q}_i, i = 1, 2, \dots, n$ .              |

i.e.,  $a_{i+1} = l_{10}([pa_i, s_{i+1}])$ . Finally, we make predictions for both the performance in the next programming exercise process and the score of the next solution using the following equations:

$$\begin{aligned} \bar{y}_{i+1} &= pred_p(a_{i+1}) \\ \bar{q}_{i+1} &= pred_s(a_{i+1}) \end{aligned} \quad (14)$$

where  $pred_p()$  and  $pred_s()$  denote prediction networks. The cross entropy loss [15] and the MSE loss [16] are used to optimize MDPAT for achieving programming ability tracing of students within the stochastic gradient descent optimization framework:

$$L = \lambda_1 CE(\bar{y}, y) + \lambda_2 (MSE(\bar{q}, q)) \quad (15)$$

where  $\lambda_1$  and  $\lambda_2$  are the hyper-parameters for weighting the cross entropy loss and the MSE loss.  $y$  and  $q$  denotes programming exercise process performance and the score of programming exercise, respectively. The detailed algorithm process is shown in the Table 1.

### 3. Results and discussion

#### 3.1. Dataset and Setup

The performance of MDPAT is evaluated via two datasets. AIZU\_Cpp dataset [3] consists of programming exercises completed by 5,268 unique students on the AIZU.org platform in C++. Collectively, these students attempted 2,206 different exercises, submitting a total of 271,189 solutions. On average, each student made about 51.48 submissions, with an average score of 0.77, closely aligning with the final submission acceptance rate of 74.30%. Atcoder\_C dataset [4] contains data from 6,282 students programming in C on Atcoder.org. These students worked on 1,670 exercises, generating a total of 425,238 submissions, with an average of 67.69 submissions per student. The average student score

is 0.62, reflecting a 62% success rate on submissions, while the acceptance rate of final submissions is notably higher at 97.17%. Following [17], to evaluate MDPAT performance, three metrics are used: AUC, ACC, and f1.

#### 3.2. Comparison with baselines

**Comparison baselines:** Six deep programming ability tracing methods are compared on the AIZU\_Cpp dataset and Atcoder\_C dataset in terms of AUC, ACC, and f1, to demonstrate the performance of MDPAT, containing Deep knowledge tracing (DKT), graph knowledge tracing (GKT), convolutional knowledge tracing (CKT), stable knowledge tracing with diagnostic transformer (SK-TDT), enhancing deep knowledge tracing (EDKT), and a pre-trained model for programming and natural languages (Codebert). DKT models interaction information between students and coursework within the RNN architecture to achieve the knowledge tracing. GKT utilizes the bipartite graph to learn programming representations and achieves the knowledge tracing within dual deep architecture. CKT devises individualized learning and common learning for student programming within the convolutional architecture to achieve the knowledge tracing. SKTDT constructs a dual transform architecture for practice and knowledge, capturing student programming knowledge status from multiple dimensions. EDKT utilizes auxiliary tasks to boost programming knowledge tracing within the deep architecture.

**Comparison results:** As shown in Table 2, MDPAT outperforms six other deep programming ability tracking methods on both the AIZU\_Cpp and Atcoder\_C datasets. Specifically, MDPAT achieves the best performance in terms of ACC (accuracy), AUC (area under the curve), and F1 (a performance metric combining precision and recall). Compared to the second-best results, ACC, AUC, and F1 scores

**Table 2.** Comparison of MDPAT on the AIZU\_Cpp and Atcoder\_C datasets

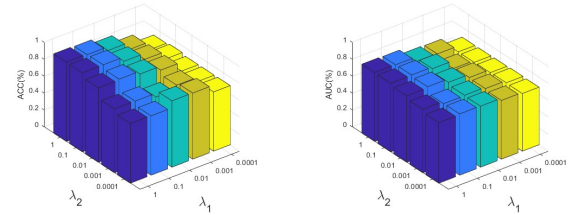
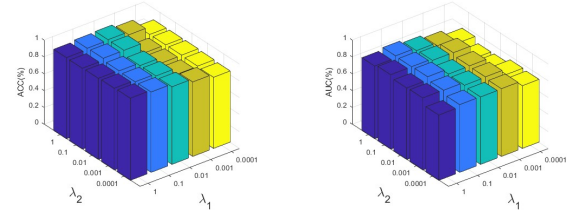
| Method        | AIZU_Cpp      |               |               | Atcoder_C     |               |               |
|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
|               | ACC           | AUC           | f1            | ACC           | AUC           | f1            |
| DKT [18]      | 0.8100        | 0.6785        | 0.8326        | 0.8312        | 0.7019        | 0.8569        |
| GKT [7]       | 0.8333        | 0.6912        | 0.8562        | 0.8674        | 0.7285        | 0.8766        |
| CKT [8]       | 0.7946        | 0.6626        | 0.8014        | 0.8155        | 0.6814        | 0.8255        |
| SKTDT [2]     | 0.8946        | 0.7811        | 0.8635        | 0.9095        | 0.8566        | 0.9592        |
| EDKT [3]      | 0.8774        | 0.7778        | 0.8551        | 0.8799        | 0.8496        | 0.9367        |
| Codebert [12] | 0.8566        | 0.7000        | 0.7933        | 0.8458        | 0.8012        | 0.8962        |
| MDPAT         | <b>0.9390</b> | <b>0.8116</b> | <b>0.8794</b> | <b>0.9601</b> | <b>0.8871</b> | <b>0.9796</b> |

of MDPAT on the AIZU\_Cpp dataset are higher by 0.0454, 0.0305, and 0.0169, respectively. On the Atcoder\_C dataset, MDPAT surpasses by 0.0359, 0.0225, and 0.0204 in ACC, AUC, and F1, respectively. This performance advantage can be attributed to three critical mechanisms: (1) MDPAT’s dual representation of both static and dynamic code features through the Programming Knowledge Graph and Programming Iteration Graph facilitates a holistic view of the underlying programming behaviors. By modeling the structural and temporal evolution of code, MDPAT enables a richer understanding of student learning patterns, leading to more precise assessments. (2) The gated update mechanism, inspired by Long Short-Term Memory (LSTM) networks, enables MDPAT to adaptively filter and update the knowledge state, selectively incorporating new submissions while maintaining continuity with prior knowledge. This dynamic retention of salient historical context supports more robust tracking of skill progression. (3) In the final prediction stage, MDPAT’s integrated framework harmonizes the representation of both programming knowledge and ability, creating a unified architecture that simultaneously accounts for conceptual mastery and practical problem-solving skills. This synergistic approach significantly enhances predictive accuracy by capturing both the theoretical understanding and applied proficiency of the learner.

### 3.3. Parameter Analysis

We analyze the effect of varying  $\lambda_1$  and  $\lambda_2$ , which are used to balance the cross entropy loss and the MSE loss, on MDPAT performance across the AIZU\_Cpp and Atcoder\_C datasets, using ACC and AUC as metrics. The results show a clear trend: as  $\lambda_1$  and  $\lambda_2$  increase within the range  $[0.0001, 1]$ , performance improves, peaking when both parameters are in the interval  $[0.1, 1]$ . In this range, the model achieves near-optimal results for both ACC and AUC. Performance is particularly strong when  $\lambda_1$  and  $\lambda_2$  are around 0.5, where a good balance between learning new knowledge and retaining past information is maintained.

However, as the values of  $\lambda_1$  and  $\lambda_2$  drop below 0.01, performance declines, indicating that small parameter values lead to excessive retention of prior knowledge or difficulty integrating new information. Thus, the optimal range for  $\lambda_1$  and  $\lambda_2$  is  $[0.1, 1]$ , where model stability and accuracy are maximized. Based on this, we set  $\lambda_1 = 0.5$  and  $\lambda_2 = 0.5$  to maintain an ideal balance between knowledge integration and retention while avoiding overfitting or underfitting.

(a) AIZU\_Cpp-ACC( $\lambda_1$  and  $\lambda_2$ ) (b) AIZU\_Cpp-AUC( $\lambda_1$  and  $\lambda_2$ )(c) Atcoder\_C-ACC( $\lambda_1$  and  $\lambda_2$ ) (d) Atcoder\_C-AUC( $\lambda_1$  and  $\lambda_2$ )**Fig. 2.** Parameter analysis of  $\lambda_1$  and  $\lambda_2$  on the AIZU\_Cpp and Atcoder\_C datasets

### 3.4. Ablation Analysis

We conduct ablation Analysis to verify component effectiveness in MDPAT. There are three ablation variants. MDPAT\_1 utilizes multigraph programming modelling and programming answer prediction to achieve the programming ability tracing. MDPAT\_2 utilizes multigraph programming modelling, programming knowledge gated update, and programming answer prediction to achieve the programming ability tracing. MDPAT\_3 utilizes multigraph programming modelling, programming ability gated

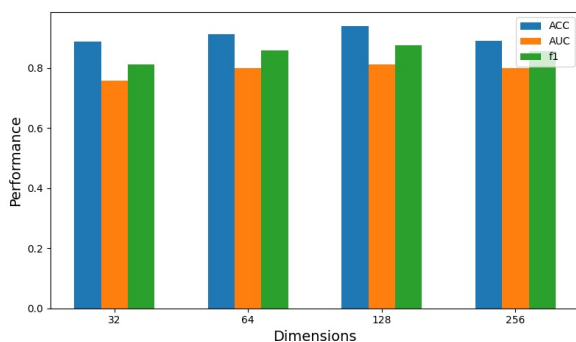
**Table 3.** Ablation Analysis of MDPAT on the AIZU\_Cpp and Atcoder\_C datasets

| Method  | AIZU_Cpp      |               |               | Atcoder_C     |               |               |
|---------|---------------|---------------|---------------|---------------|---------------|---------------|
|         | ACC           | AUC           | f1            | ACC           | AUC           | f1            |
| MDPAT_1 | 0.8400        | 0.6799        | 0.8111        | 0.8685        | 0.7991        | 0.8956        |
| MDPAT_2 | 0.8833        | 0.7854        | 0.8426        | 0.8847        | 0.8308        | 0.9006        |
| MDPAT_3 | 0.8545        | 0.7712        | 0.8033        | 0.8678        | 0.8077        | 0.8888        |
| MDPAT   | <b>0.9390</b> | <b>0.8116</b> | <b>0.8794</b> | <b>0.9601</b> | <b>0.8871</b> | <b>0.9796</b> |

update, and programming answer prediction to achieve the programming ability tracing.

As shown in Table 3, the complete MDPAT model significantly outperforms all ablation variants across both the AIZU\_Cpp and Atcoder\_C datasets, particularly in terms of ACC, AUC, and f1 score. This indicates that the inclusion of all key components—multigraph programming modeling, the gated update mechanisms for both programming knowledge and ability, and programming answer prediction—contributes to the overall superior performance of the model. For instance, the full MDPAT model achieves an ACC of 0.9390 and an AUC of 0.8116 on the AIZU\_Cpp dataset, surpassing MDPAT\_2 and MDPAT\_3, which lack the full gated update mechanism, by significant margins. Similarly, on the Atcoder\_C dataset, the full MDPAT reaches an ACC of 0.9601 and an AUC of 0.8871, demonstrating its robustness across different datasets. These results highlight the critical role of each component, particularly the gated update mechanisms, in enabling the model to effectively capture and trace students' programming knowledge and ability over time, leading to more accurate and reliable predictions.

### 3.5. Dimensionality Analysis



**Fig. 3.** Dimensionality impact on performance on the AIZU\_Cpp

The impact of dimensionality on programming ability metrics is illustrated in Fig. 3. As the dimensionality increases, we observe notable variations in the performance

metrics, including accuracy (ACC), area under the curve (AUC), and F1 score. For the dimensions tested, specifically 32, 64, 128, and 256, the accuracy values show a general upward trend, peaking at a dimensionality of 128 with an accuracy of 0.939. However, at 256 dimensions, there is a slight decline to 0.890. This indicates that while a moderate increase in dimensionality can enhance the model's ability to capture relevant features, excessive dimensions may lead to overfitting or increased noise, adversely affecting performance. Similar trends are observed in the AUC and F1 scores. The AUC improves from 0.7569 at 32 dimensions to a maximum of 0.8112 at 128 dimensions, before slightly decreasing to 0.800 at 256. The F1 score reflects a comparable pattern, rising from 0.8129 to 0.8749 and then dropping to 0.8569 at the highest dimensionality. These findings suggest that there exists an optimal range of dimensionality that maximizes programming ability metrics. Specifically, 128 dimensions appear to balance the trade-off between model complexity and generalization ability, leading to superior performance in measuring programming skills.

### 4. Conclusion

In this paper, we present MDPAT, a novel multigraph-based method for tracing programming ability in vocational college students. By capturing both static and dynamic aspects of programming activities, MDPAT offers a more nuanced assessment of proficiency. Utilizing the Programming Knowledge Graph and the Programming Iteration Graph, MDPAT models the structural and evolutionary features of code. Inspired by LSTM networks, it employs gated update mechanisms for programming knowledge and ability, allowing for selective integration of new information while retaining essential prior knowledge. MDPAT enhances prediction accuracy in programming exercises and outperforms state-of-the-art methods, achieving a 5.06% accuracy improvement on the Atcoder\_C dataset. Ablation studies highlight the importance of balancing feature representation and knowledge integration. MDPAT advances programming ability assessment, providing detailed proficiency tracking. In future work, we plan to explore the integration of contextual factors such as problem difficulty and

learning behaviors, as well as extend MDPAT to support additional programming languages and diverse educational environment.

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